

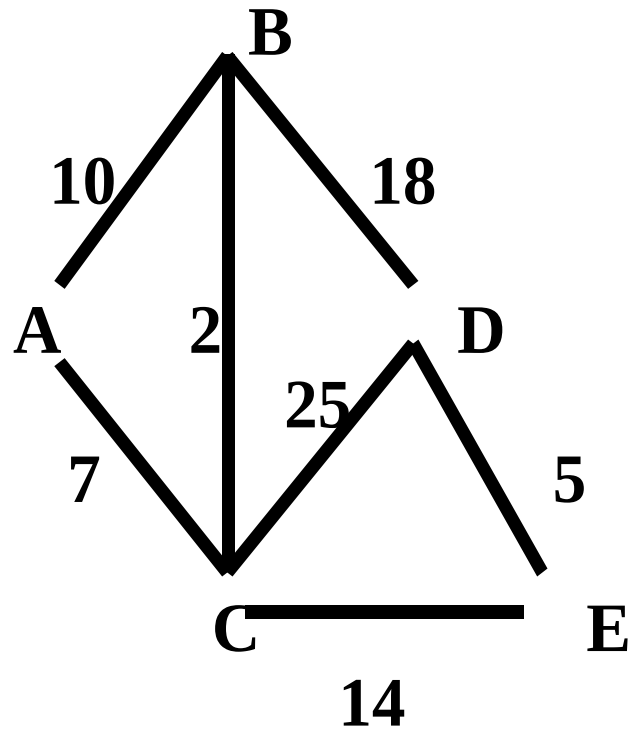
Dijkstra's algorithm:

Let pq be a priority queue of vertex-weight pairs, $\langle w, \text{wweight} \rangle$, where wweight is the **total** weight of all edges on the shortest path so far from v1 to w.

Iterate, breadth-first, starting at v1 until a pair with v2 is removed from pq.

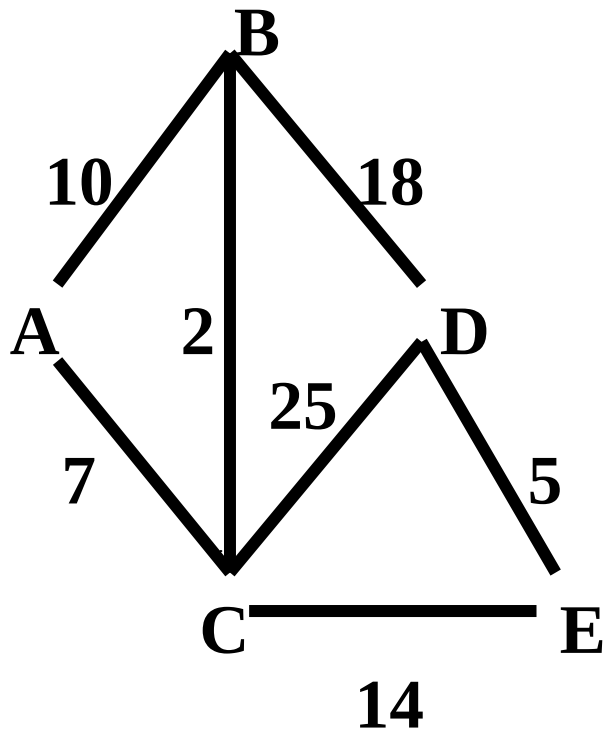
To keep track of total path weights, we have a Map object, `weightSum`, that associates with each vertex x the sum of the weights on the shortest path so far from v_1 to x .

Finally, **predecessor**, another Map object, associates each vertex x with its predecessor on the shortest path so far from v_1 to x . That map enables us to retrieve the shortest path when we are done.



Find the shortest path from A to D.

**Initialize weightSum and predecessor,
and add $\langle A, 0 \rangle$ to pq.**

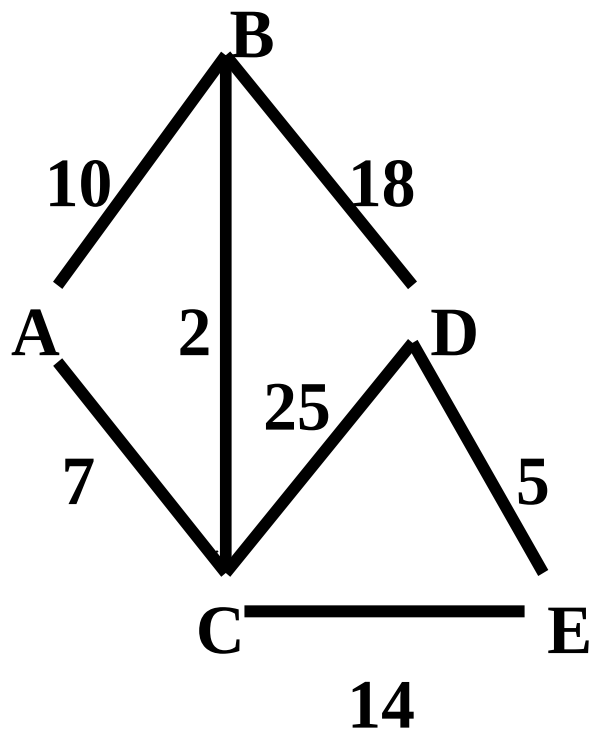


<u>weightSum</u>	<u>predecessor</u>	<u>pq</u>
A, 0	A	<A, 0>
B, 1000	null	
C, 1000	null	
D, 1000	null	
E, 1000	null	

Now loop until D is removed from pq. For each pair $\langle w, \text{weight sum} \rangle$ removed from pq, iterate over the neighbors of w (provided that weight sum is $\leq w$'s weight sum).

For each neighbor x, if w 's weight sum + weight of (w, x) is less than x 's weight sum, then we have found a cheaper way to get from A to x!

**So replace x 's weight sum with w 's weight sum + weight of (w, x) and insert x and its new weight sum into pq.
Also, make w the predecessor of x .**



weightSum

A, 0

B, 10

C, 7

D, 1000

E, 1000

predecessor

A

A

A

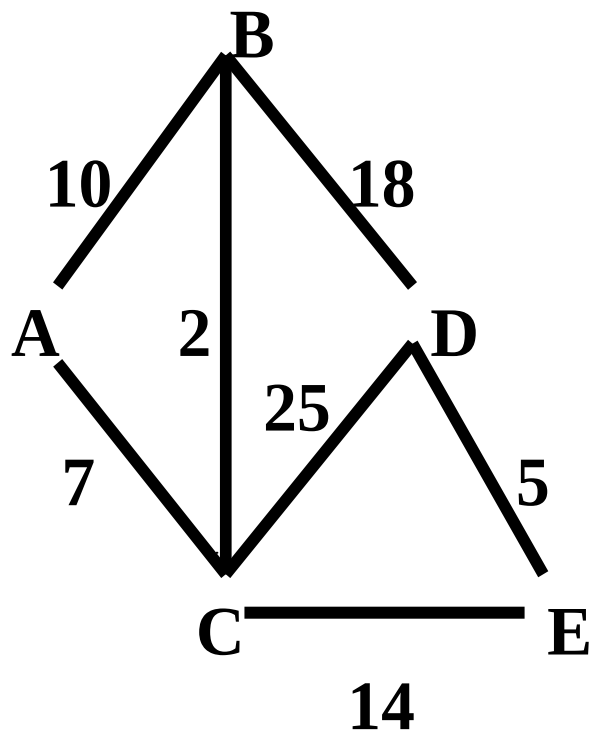
null

null

pq

<C, 7>

<B, 10>



weightSum

A, 0

B, 9

C, 7

D, 32

E, 21

predecessor

A

C

A

C

C

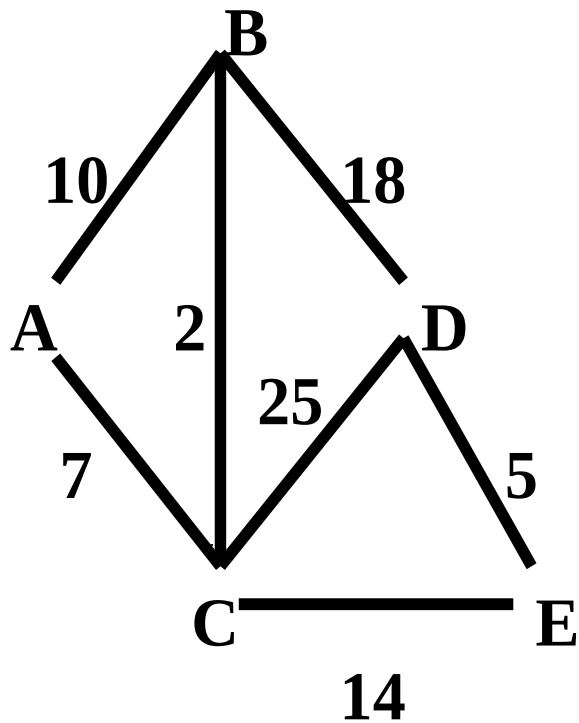
pq

<B, 9>

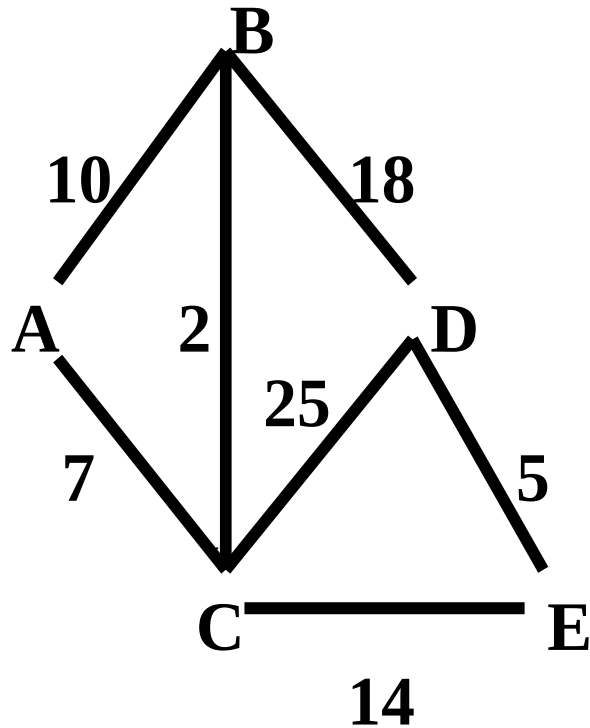
<B, 10>

<E, 21>

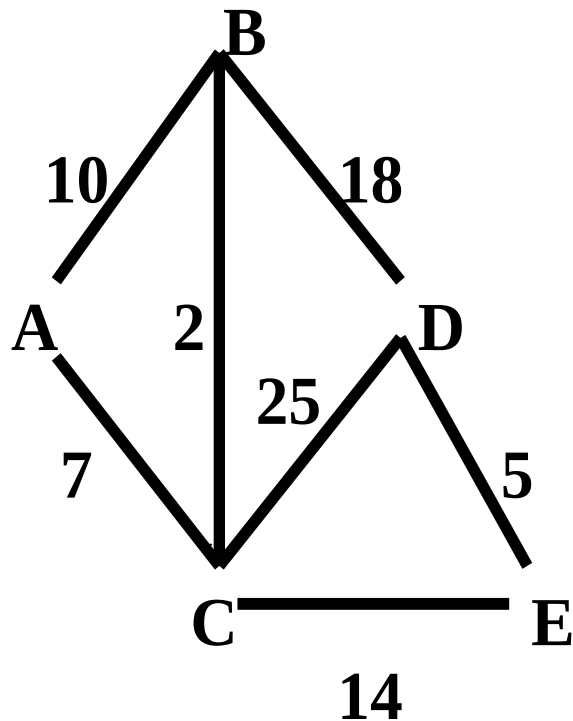
<D, 32>



<u>weightSum</u>	<u>predecessor</u>	<u>pq</u>
A, 0	A	
B, 9	C	<E, 21>
C, 7	A	<D, 27>
D, 27	B	<D, 32>
E, 21	C	



<u>weightSum</u>	<u>predecessor</u>	<u>pq</u>
A, 0	A	<E, 21>
B, 9	C	<D, 27>
C, 7	A	<D, 32>
D, 27	B	
E, 21	C	



<u>weightSum</u>	<u>predecessor</u>	<u>pq</u>
A, 0	A	<D, 26>
B, 9	C	<D, 27>
C, 7	A	<D, 32>
D, 26	E	
E, 21	C	

During the next loop iteration, when <D, 26> is removed from pq, we stop. The shortest path from A to D is, according to predecessor, A, C, E, D.